

5.6 Solving Exponential and Logarithmic Equations

Solving WITHOUT a calculator.

Like Bases (or Bases that can be made like)

Solve each exponential or logarithmic equation.

1) $7^{2x} = 7^{48}$

2) $25^{4x} = 125^{2x-1}$

3) $2^{x+3} = 8^{x-1}$

4) $\log_2(x + 6) = \log_2(10x)$

5) $\log x + \log(x - 4) = \log 45$

But... what happens if we cannot make the bases the same?

1) $8^x = 44$

2) $2 - 6^x = -9$

3) $8e^{2x} = 20$

4) $e^{x+7} = 10$

5) $3^{x+2} = 7$

6) $4^{2x-1} = 3^{x+5}$

7) $5^{x+4} = 3^{4x-3}$

When there is ONE Logarithm (or you can condense to get a single logarithm)

Examples)

1.) $\log_2(x + 1) - 2 = 5$

2) $6 - \log(3x) = -2$

3.) $2 \log(x) - \log(3) = 2$

4) $\ln x + \ln 3 = 2$

5) $4 + 3 \log(2x) = 16$

Practice:

1) $2 \ln(x + 6) = -18$

2) $4^x = \left(\frac{1}{2}\right)^{x-3}$

3) $\log(2x) = 2 - \log(x - 5)$

4) $\log_3(7x + 1) - \log_3(x - 2) = 2$

5) $\log_4 2x + \log_4 3 = \log_4 36 - \log_4 2$

6) $2 \ln x = \ln 2 + \ln(3x - 4)$

7) $6^{3x-4} = 10^{2x}$

8) $9^{4x-1} = 27^{2x+5}$

9) $5 \ln(2x - 1) = -25$

10) $\log_2(n^2 + 12) = \log_2(-9n - 2)$